

Dipolar and scalar ${}^3\text{He}$ - ${}^{129}\text{Xe}$ frequency shifts in mm-sized stemless cells

arxiv.org/abs/1805.11578

DAMOP 2018, Ft. Lauderdale (Thurs. May 31, 2:48, Grand F)

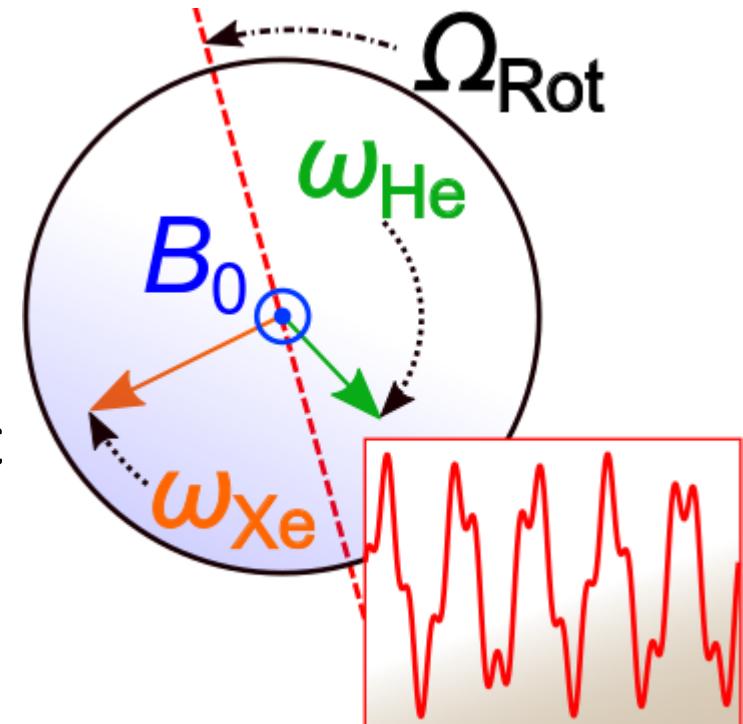
Mark Limes, Nezih Dural, Mike Romalis, Princeton University

Elizabeth Foley, Tom Kornack, Allan Nelson &

Larry Grisham, Twinleaf LLC



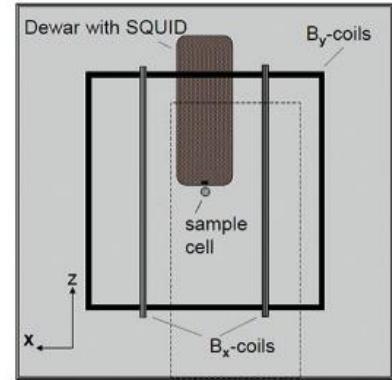
Twinleaf



$$f_r = \frac{\gamma_{\text{He}} B_0 \pm \Omega}{\gamma_{\text{Xe}} B_0 \pm \Omega}$$

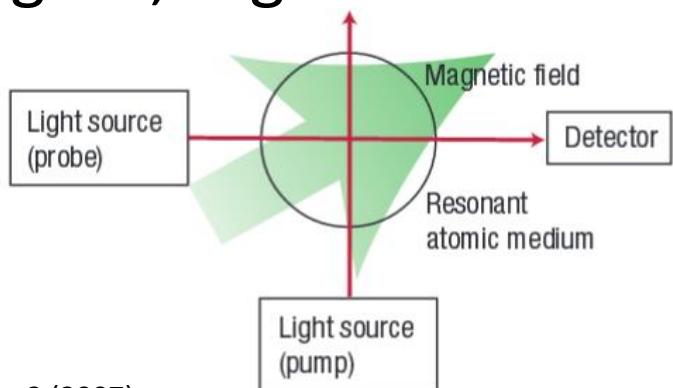
Dual Nuclear-spin Comag. detection

- SQUIDs: Good sensitivity H06 : 9 Terrano, Meinel, Sachdeva, Chupp
Detects dipolar field of ${}^3\text{He}-{}^{129}\text{Xe}$ outside sphere



Heil, et al., Ann. Phys. (Berlin) 525 (2013), etc.!

- Alkali Magnetometer
No Cryogens, High SNR: wavefn. overlap

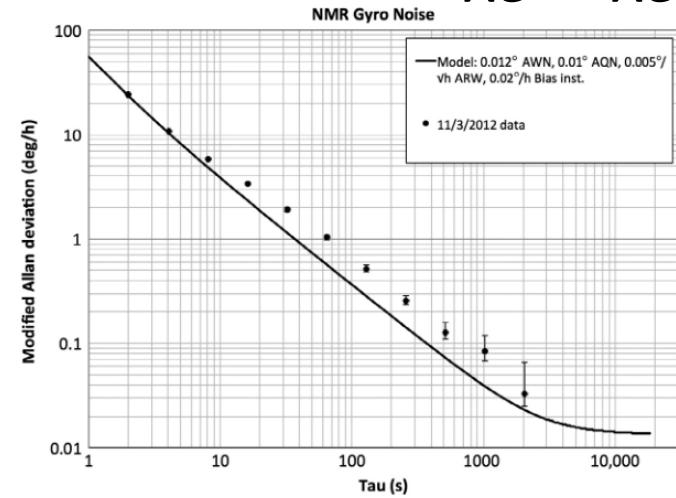


Budker, Romalis, Nature Physics, 3 (2007)

D. Sheng, A. Kabcenell, and M.V. Romalis. *Phys. Rev. Lett.* **113**, 163002 (2014)

T. W. Kornack, R. K. Ghosh and M. V. Romalis. *Phys. Rev. Lett.* **95**, 230801 (2005)

S08 : 2 Thrasher, Sorensen, Weber, Korver, Walker
 ${}^{129}\text{Xe}-{}^{131}\text{Xe}$ NMR gyro

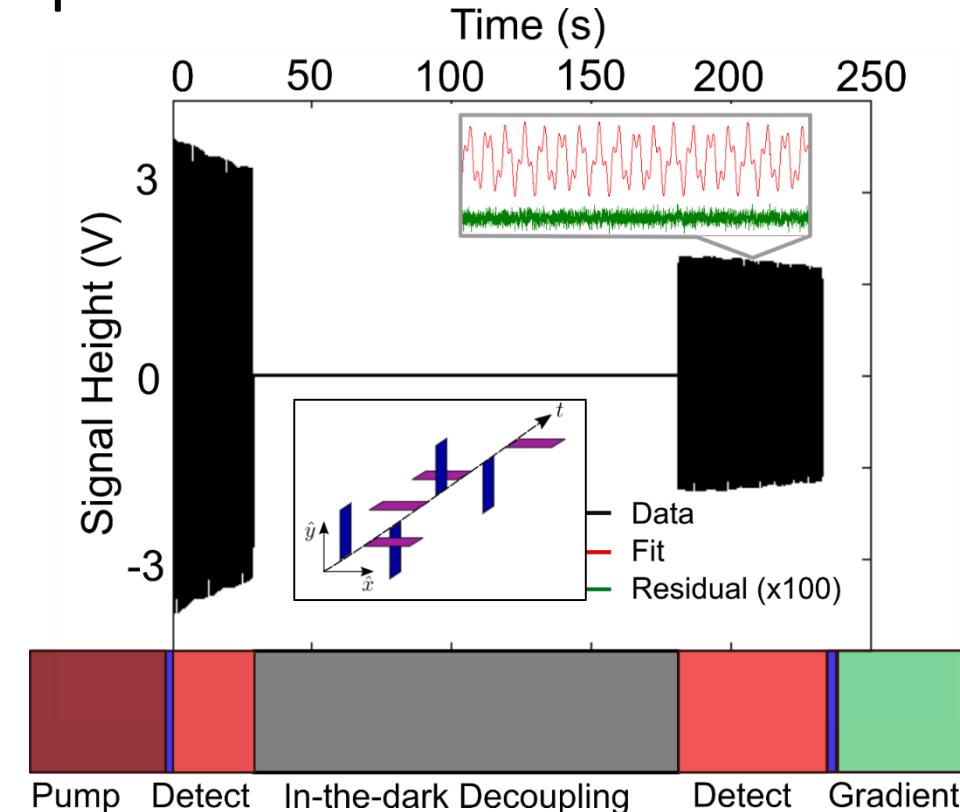
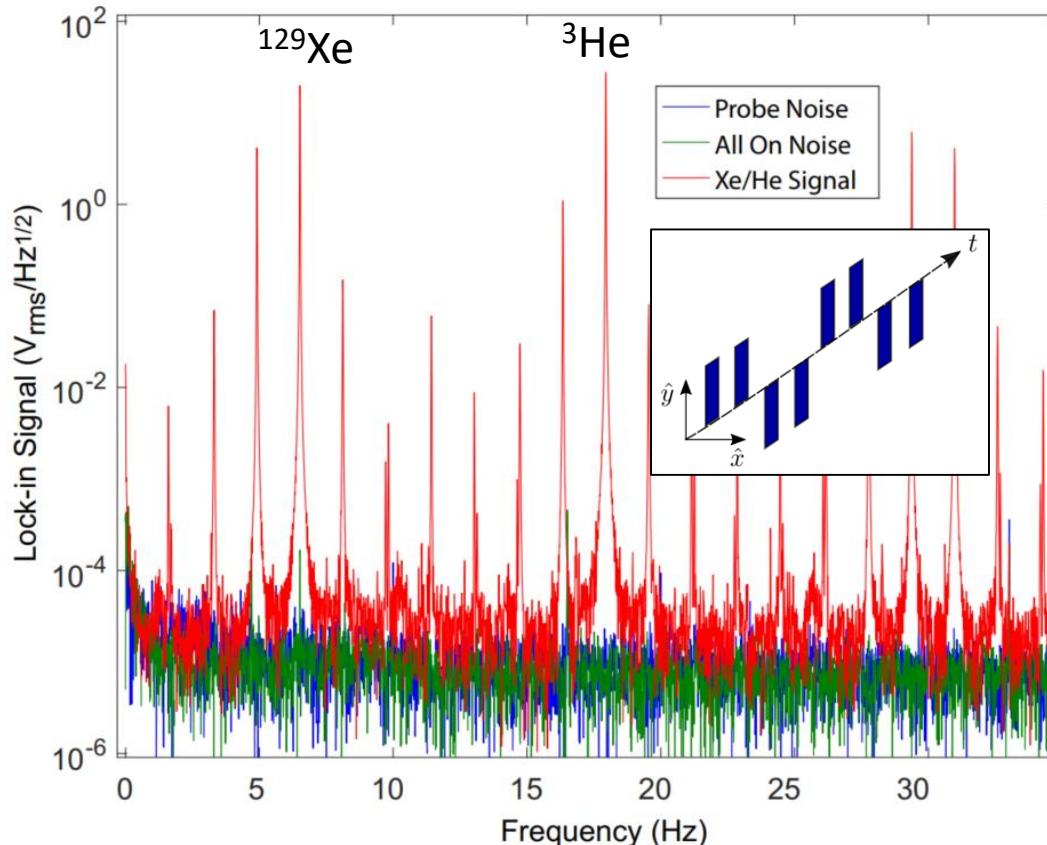


T. Walker, M. Larsen, *Advances In Atomic, Molecular, and Optical Physics*, 65 (2016)
A. Korver, D. Thrasher, M. Bulatowicz, and T. G. Walker, *Phys. Rev. Lett.* **115**, 253001 (2015)
M. Bulatowicz, R. Griffith, M. Larsen, J. Mirijanian, C. B. Fu, E. Smith, W. M. Snow, H. Yan, and T. G. Walker, *Phys. Rev. Lett.* **111**, 102001 (2013)

Gist

$$\Delta\omega_{\text{NG}} \propto -\kappa_0[\text{Rb}]\langle S_z \rangle \quad (\kappa_0)_{\text{RbHe}} = 5 \quad (\kappa_0)_{\text{RbXe}} = 500$$

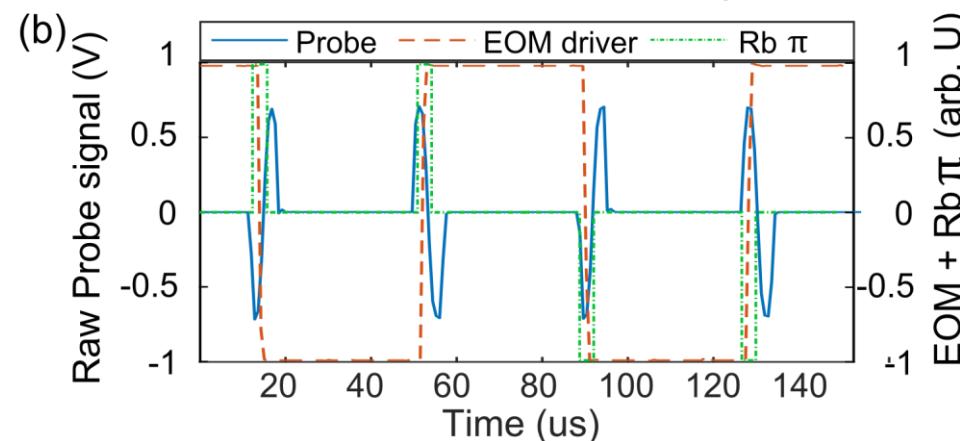
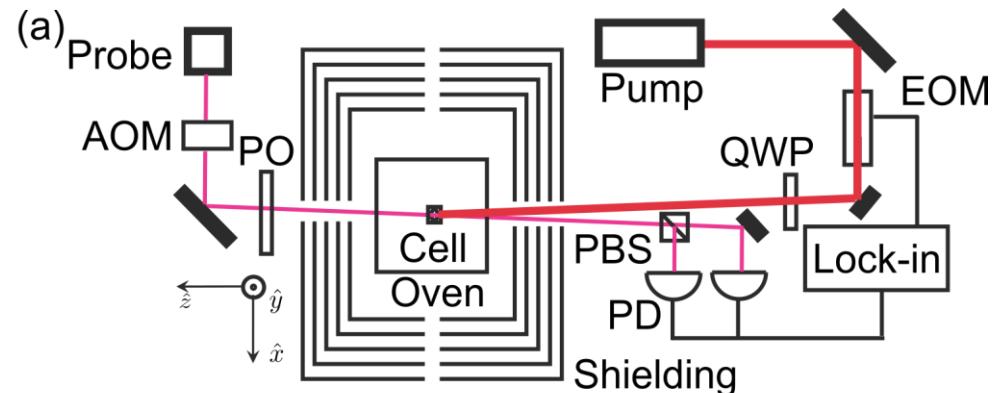
- We need to mitigate differential frequency shifts due to polarized Rb!
- 1) Pulse-train ^{87}Rb magnetometer -> **High SNR Detection of ^3He - ^{129}Xe**
- 2) Ramsey scheme with rotating ^{87}Rb pulse train -> **Precise + Accurate**



Anodically bonded cells

Liew, Knappe, Moreland, Robinson, Hollberg, Kitching, Appl. Phys. Lett. 84, 2694 (2004)

- 1) Single-axis pump/probe scheme
- 2) Record ^{129}Xe lifetimes for mm-sized cells

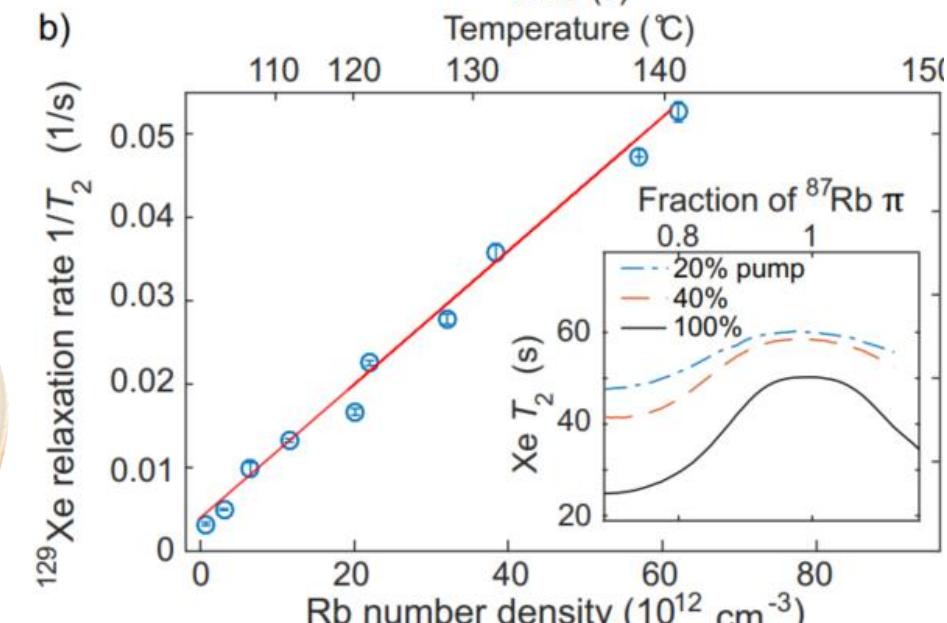
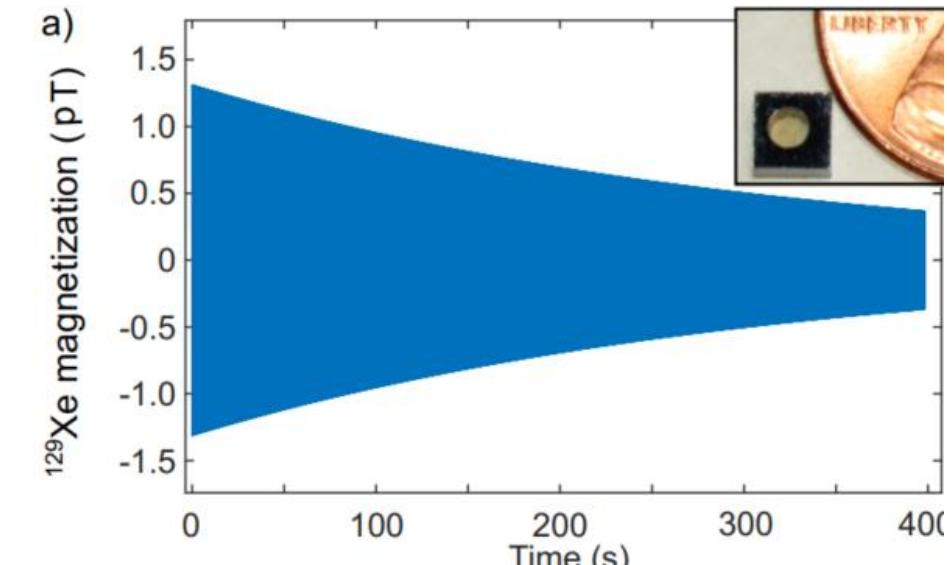


**6 mm³
active volume**



arxiv.org/abs/1805.11578

$^{129}\text{Xe} \sim 5 \text{ torr}$, $^3\text{He} \sim 1000 \text{ torr}$, N_2 - ^{87}Rb
 $^{129}\text{Xe } T_w \sim 300 \text{ s}$, $^3\text{He } T_2 \sim 4 \text{ h}$



Dipolar fields (NMR shape effect)

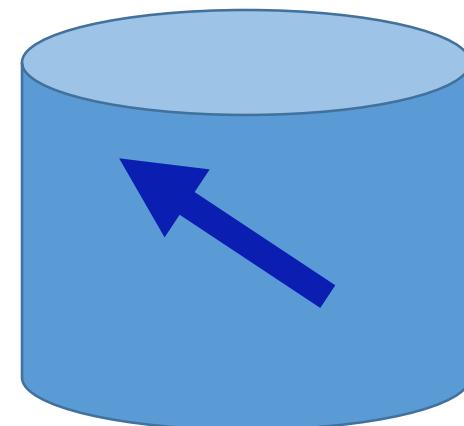
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- Spherical cells null classical dipolar fields
 - Glass blown spheres imperfect, stems need plugged
- There also exists a **cylinder size** $h/d = 0.9065$, dipolar effect vanishes!
 - Anodically bonded cells have very well-defined geometries

$$B_{dip}(\hat{r}) = \frac{3\hat{r}(\hat{r} \cdot m) - m}{r^3}$$

$$B_{con} = \frac{8\pi\kappa}{3} M_{He}$$

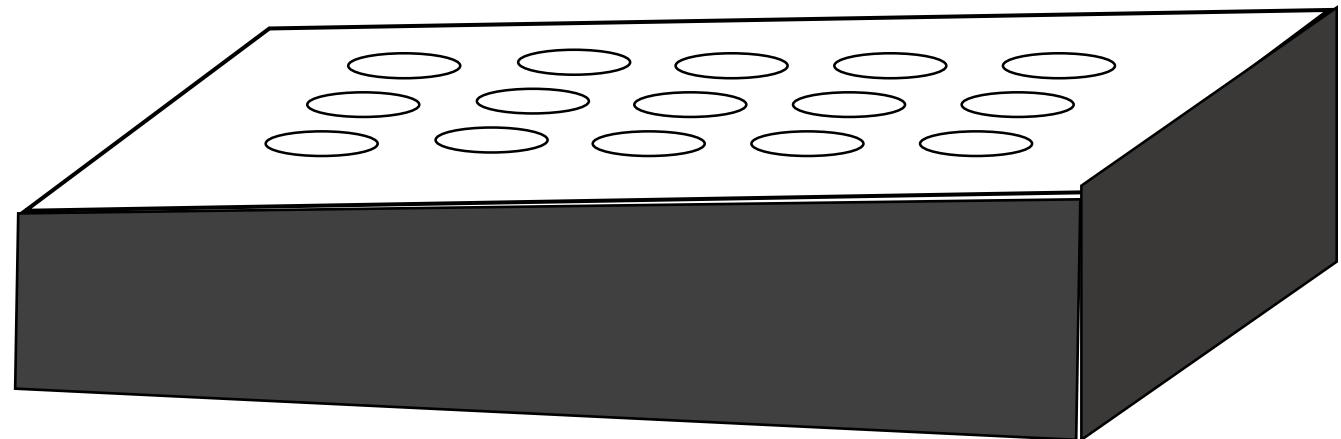
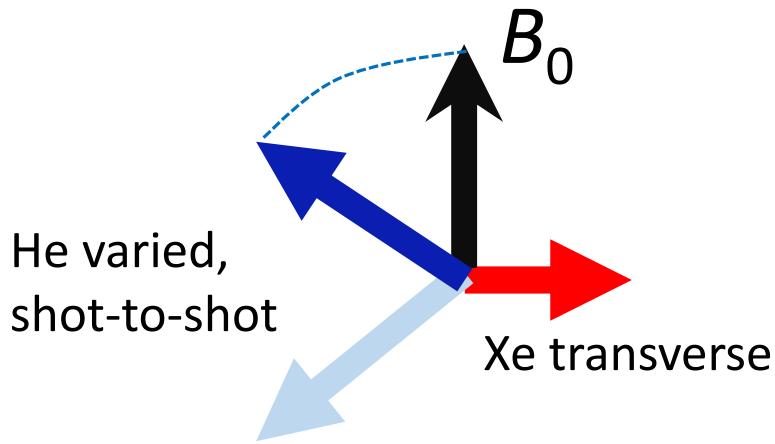


uniform density of dipoles, $n=M/m$

Dipolar fields (NMR shape effect)

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- Experiment: Vary projection of ${}^3\text{He}$ M on B_0 , and vary cell size



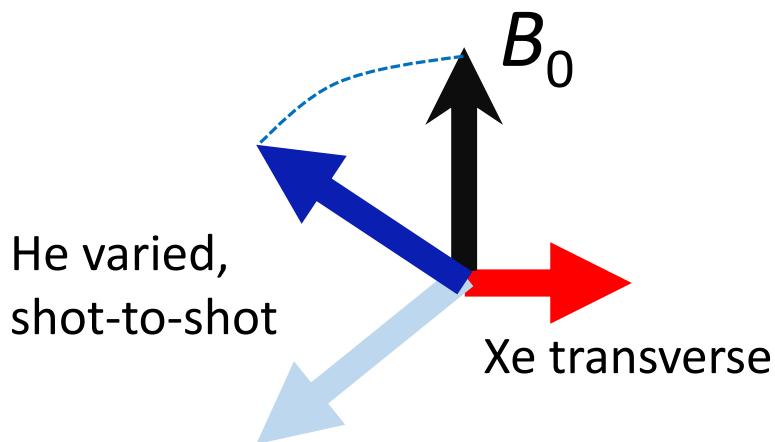
For different cell sizes, anodically bond
with graded silicon wafers,
Get cells with sizes about $h/d = 0.9065$

$$f_r - \gamma_r = \frac{\omega_{He}}{\omega_{Xe}} - \frac{\gamma_{He}}{\gamma_{Xe}}$$

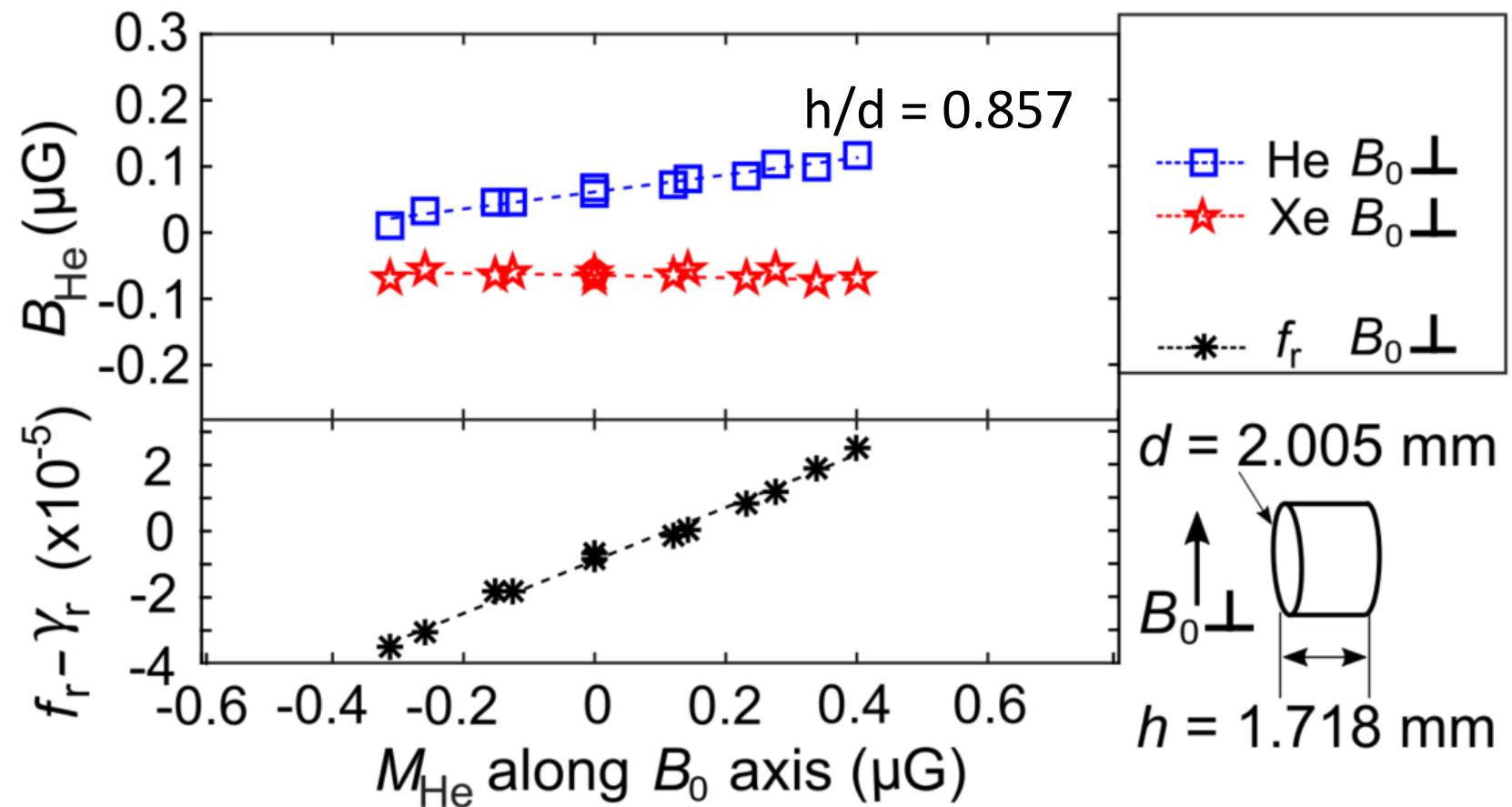
Experiment

arxiv.org/abs/1805.11578

- Vary projection of ${}^3\text{He}$ M on bias field B_0 axis



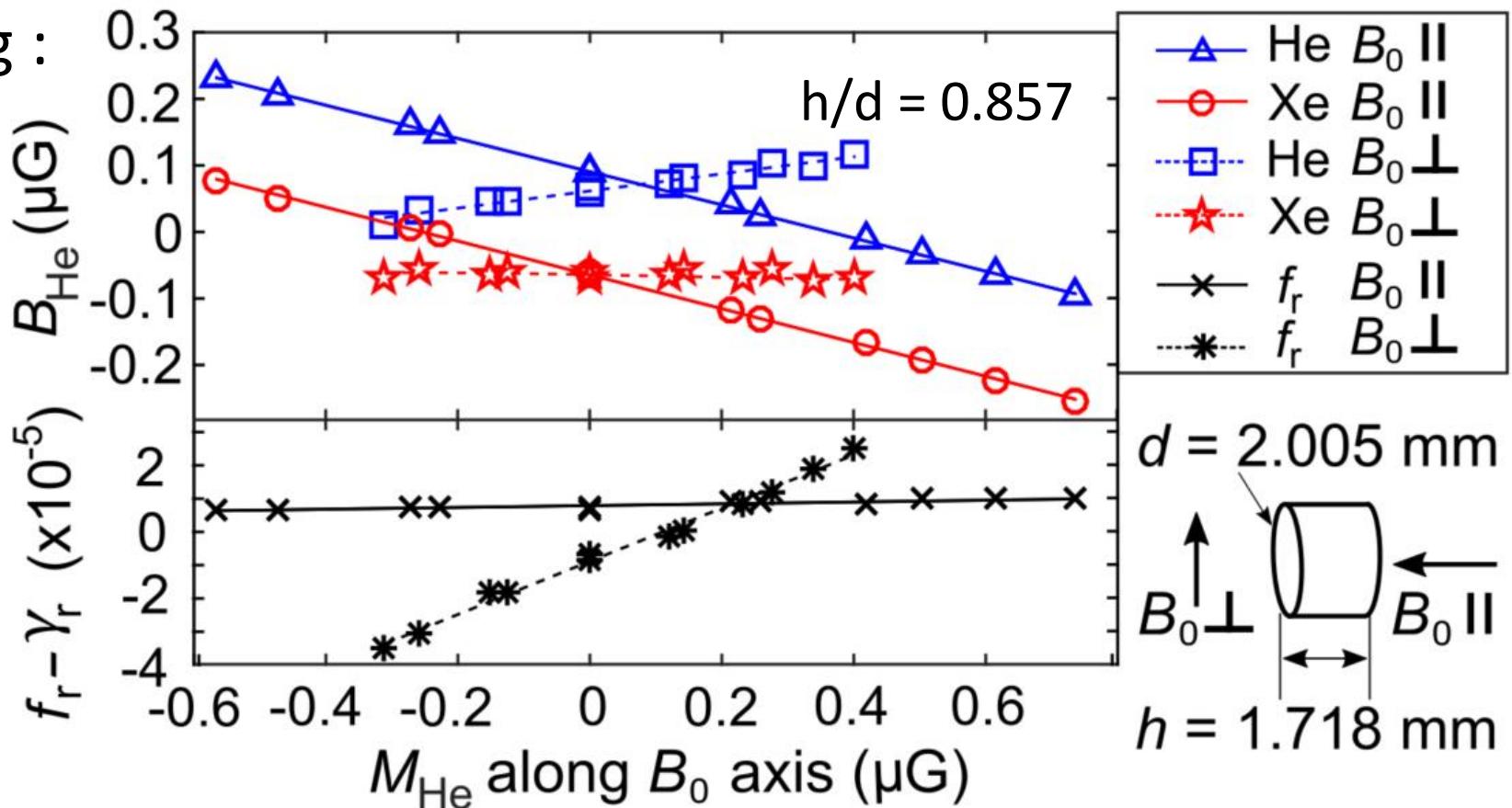
$$f_r - \gamma_r = \frac{\omega_{He}}{\omega_{Xe}} - \frac{\gamma_{He}}{\gamma_{Xe}}$$



Field experienced due to M_{He} v. orientation

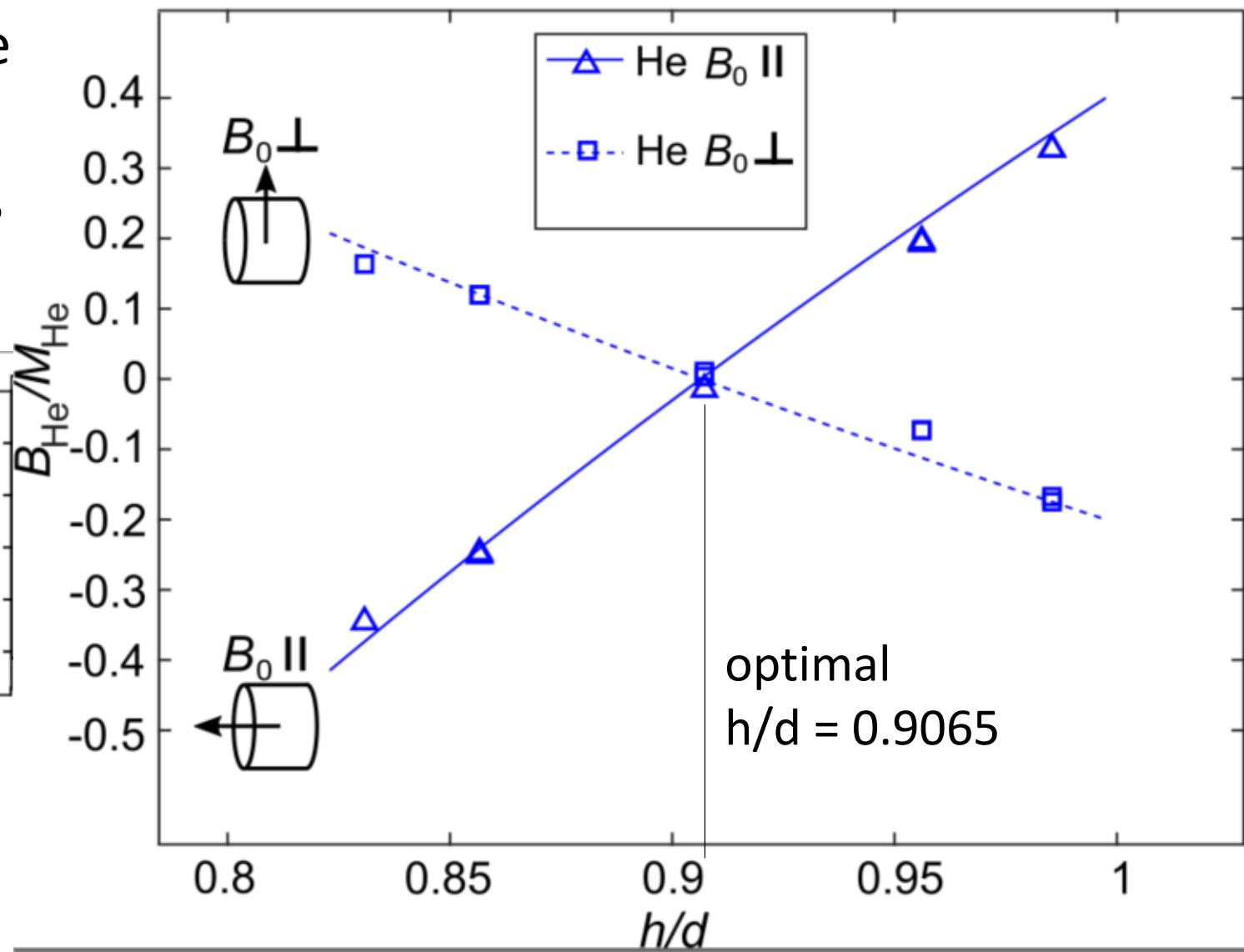
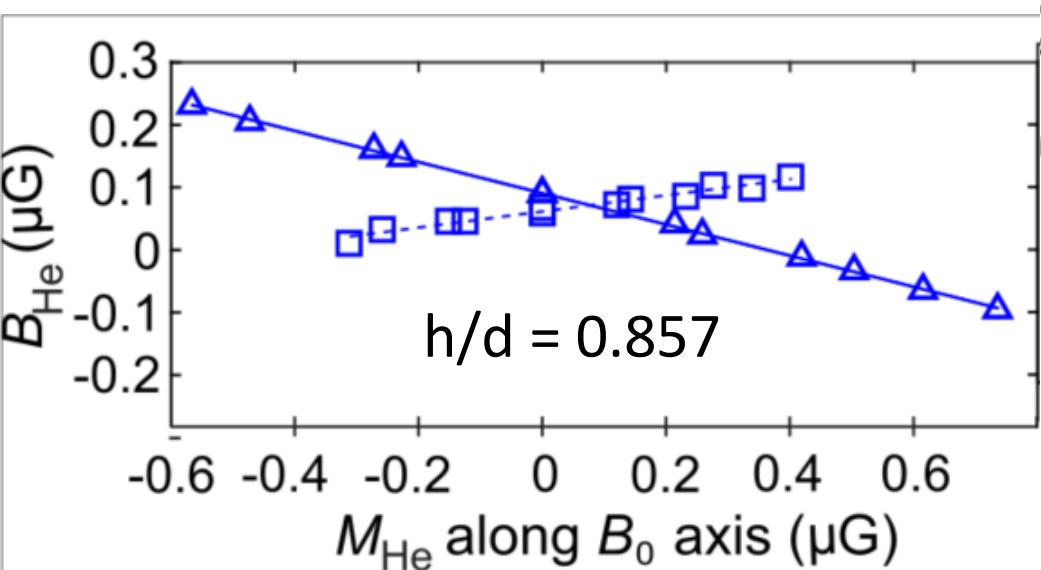
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- Plot slopes v. cylinder dimension with B_0 perp and para to cylinder axis
- f_r Sensitivity to He tipping :
- 1) Zeroed out for $h/d = 0.857\dots$
- 2) Not at theoretical value of $h/d = 0.9065$
- 3) Depends on orientation w.r.t. B_0



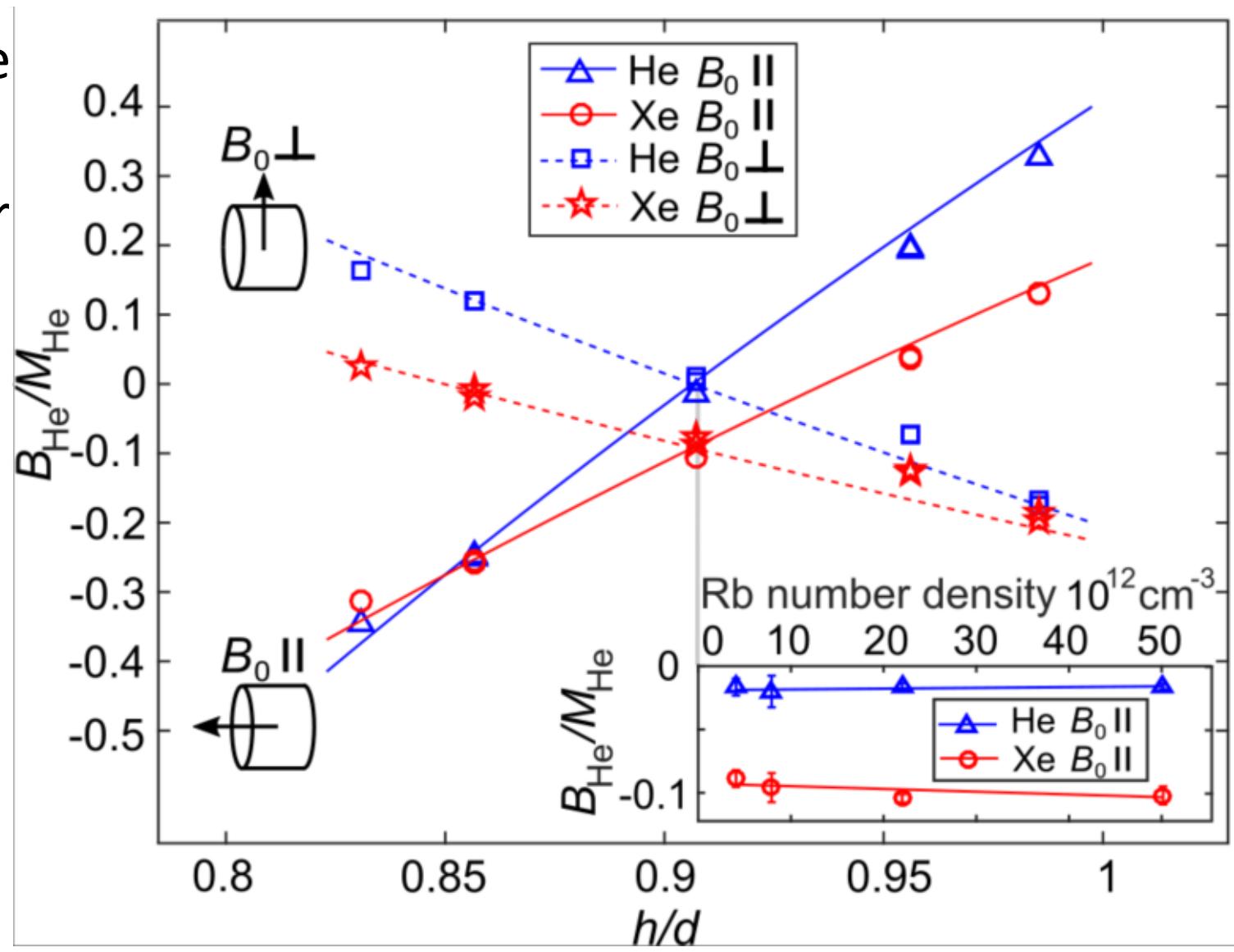
Field experienced by ${}^3\text{He}$ due to M_{He} v. cylinder size

- $h/d = 0.9065$ is a cylinder where the dipolar field should vanish
- Theory with no free parameters



Field experienced by ^{129}Xe due to M_{He} v. cylinder size

- $h/d = 0.9065$ is a cylinder where the dipolar field should vanish
- Theory with one free parameter
- ^{129}Xe shifted...
- Independent of Rb density



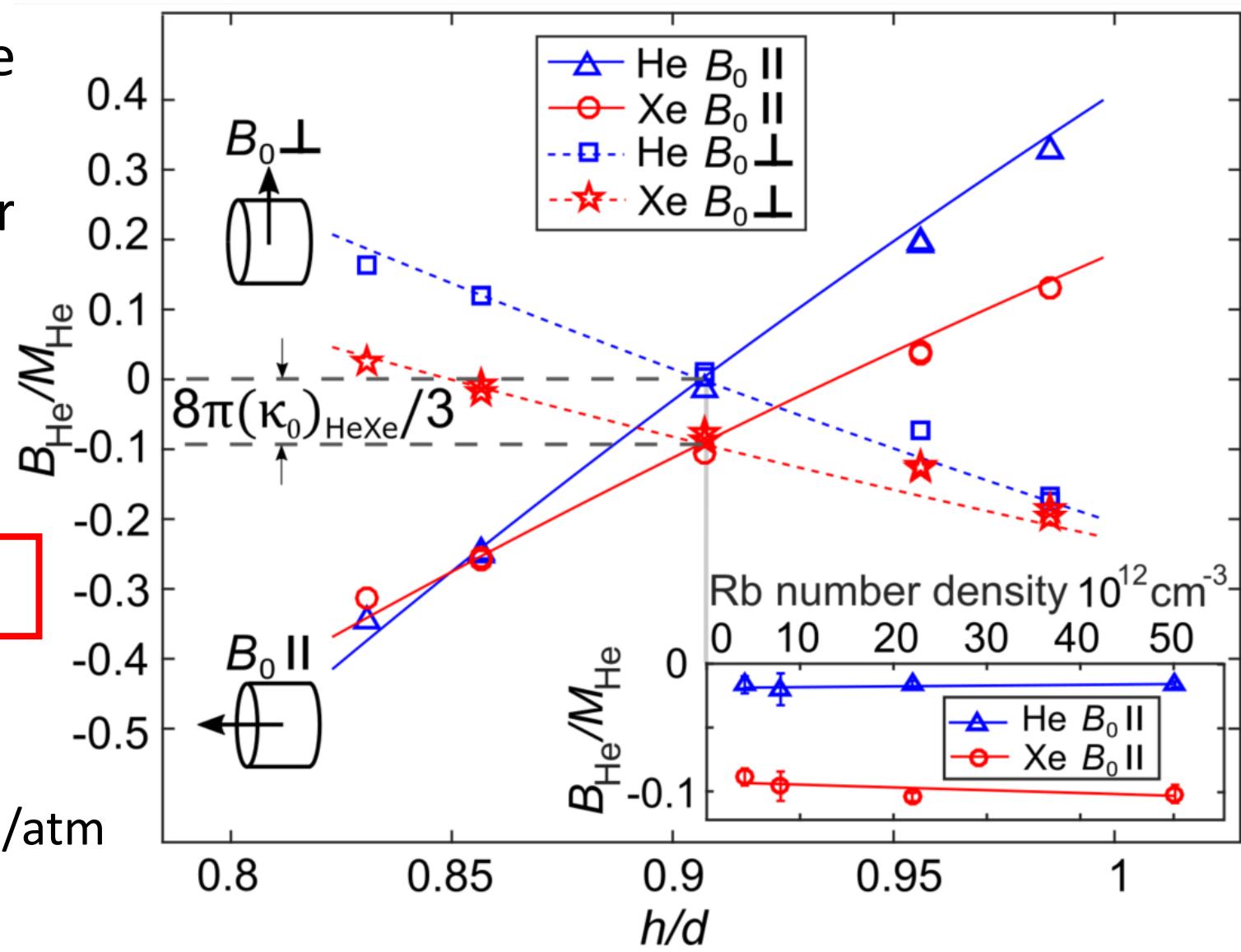
^{129}Xe experiences scalar field from ^3He

- $h/d = 0.9065$ is a cylinder where the dipolar field should vanish
- Theory with one free parameter
- ^{129}Xe shifted...
- Independent of Rb density
- $B_{dipole} + B_{contact}!$

$$\kappa_{\text{HeXe}} = -0.011 \pm 0.001$$

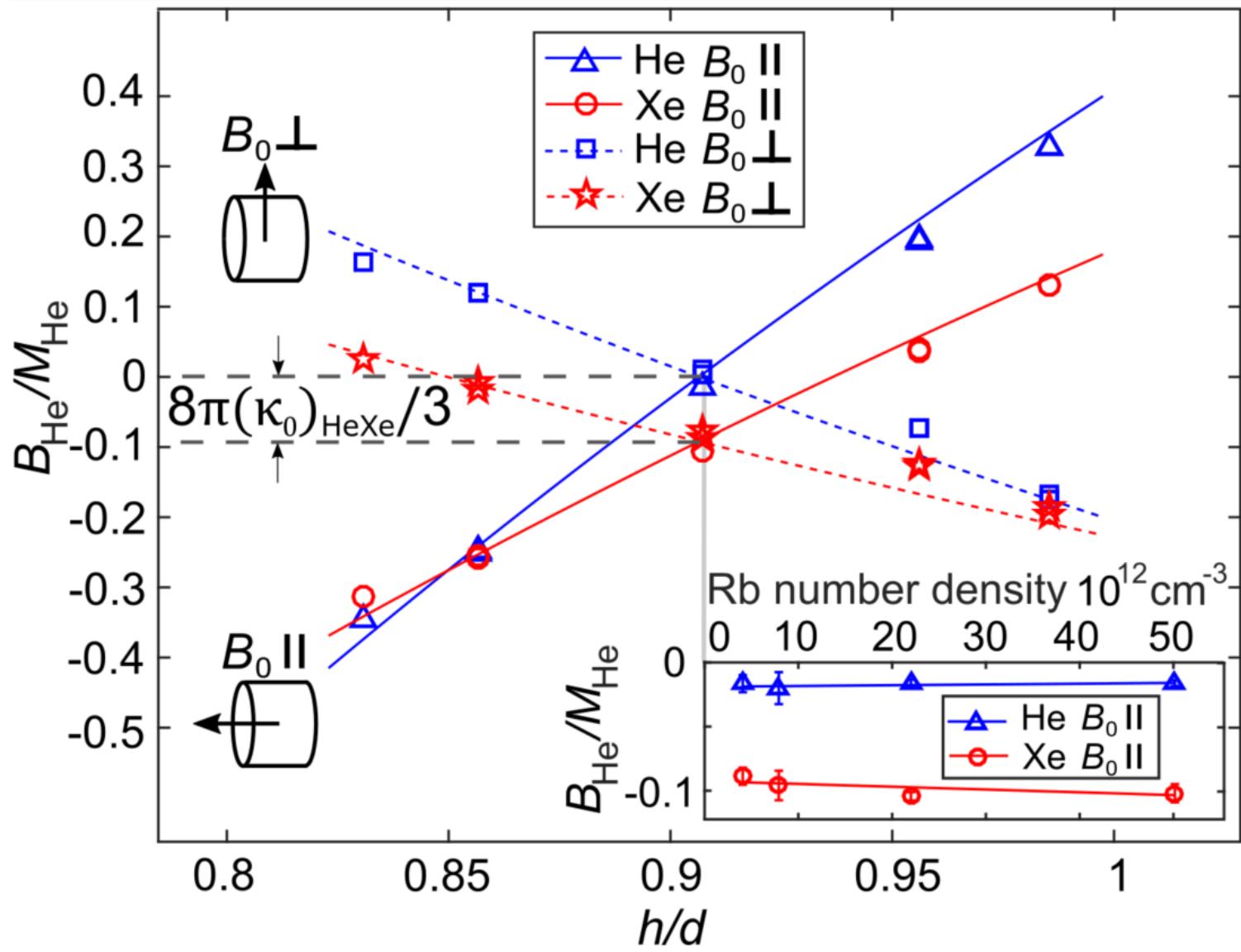
$$H = \overrightarrow{J I_{\text{He}}} \cdot \overrightarrow{I_{\text{Xe}}}$$

$$\frac{J}{P_{\text{He}}} = \frac{8}{3} \gamma_{\text{Xe}} \mu_{\text{He}} n_0 = -62 \text{ mHz/atm}$$



A few practical take-aways from κ_{HeXe}

- J coupling between gases!
- Null projection of He on bias field (good tipping pulses)
- To null frequency ratio dep., consider cylinder size, orientation w.r.t. bias field
- A **perfectly spherical** comagnetometer cell *is sensitive* to imperfect tipping pulses

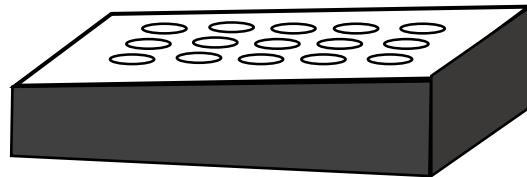


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$$f_r = \frac{\omega_{He} \pm \Omega}{\omega_{Xe} \pm \Omega}$$

- Precise and Accurate Detection with ${}^{87}\text{Rb}$ pi Pulse-trains + Ramsey
- Single-axis pump/probe, 300 s Xe wall time in anodically bonded cell
- Control and null classical dipolar fields $h/d = 0.9065$

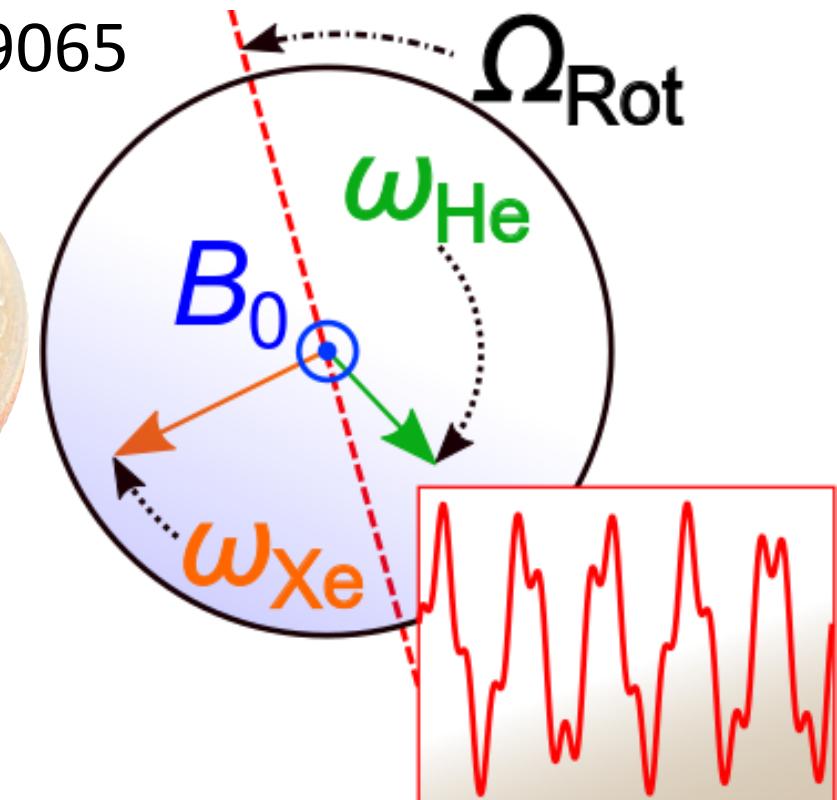


6 mm³
active volume



- Observed ${}^3\text{He}$ - ${}^{129}\text{Xe}$ J-coupling

$$\kappa_{\text{HeXe}} = -0.011 \pm 0.001$$





PRINCETON
UNIVERSITY

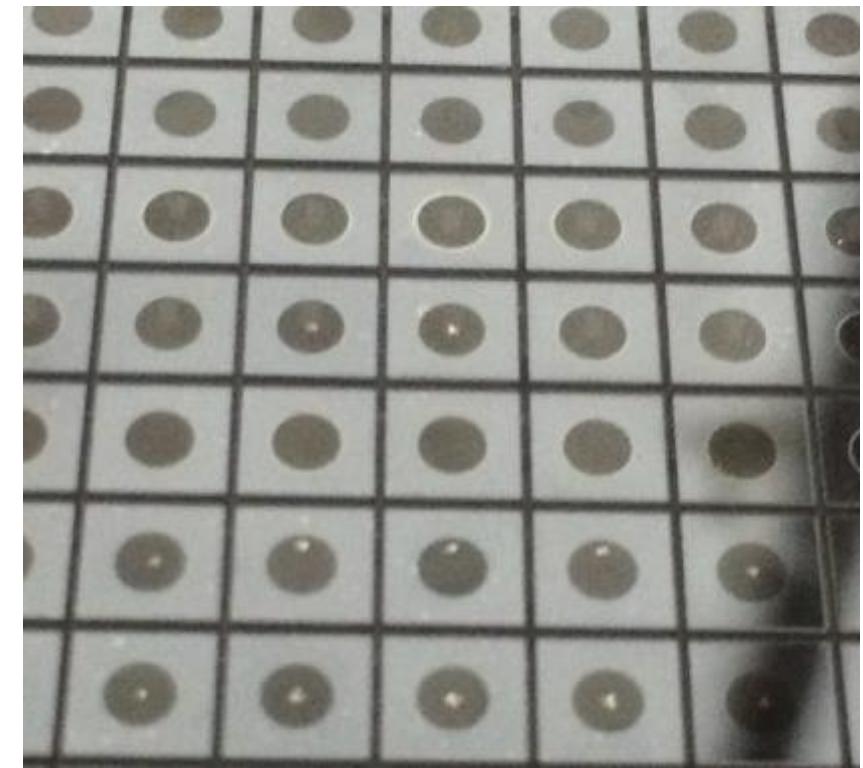


Romalis group

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Thanks!



Contact- info@twinleaf.com
if you have interesting
uses for bonded cells